

RESEARCH ARTICLE

An analysis of 3D knee kinematic data complexity in knee osteoarthritis and asymptomatic controls

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Abstract

Three-dimensional (3D) knee kinematic data, measuring flexion/extension, abduction/adduction, and internal/external rotation angle variations during locomotion, provide essential information to diagnose, classify, and treat musculoskeletal knee pathologies. However, and so across genders, the curse of dimensionality, intra-class high variability, and inter-class proximity make this data usually difficult to interpret, particularly in tasks such as knee pathology classification. The purpose of this study is to use data complexity analysis to get some insight into this difficulty. Using 3D knee kinematic measurements recorded from osteoarthritis and asymptomatic subjects, we evaluated both *single feature complexity*, where each feature is taken individually, and *global feature complexity*, where features are *considered simultaneously*. These evaluations afford a characterization of data complexity independent of the used classifier and, therefore, provide information as to the level of classification performance one can expect. Comparative results, using reference databases, reveal that knee kinematic data are highly complex, and thus foretell the difficulty of knee pathology classification.

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Data Availability Statement: The participants data are of the confidential category and cannot be put in an open repository for unrestricted public access. This restriction is imposed by the ethics committee of the University of Montreal Hospital Research Center. However, they can be made available upon request provided a statement of confidentiality is signed. Please contact the Quality system manager Caroline Lau (Caroline.Lau@etsmtl.ca).

Introduction

Three-dimensional (3D) knee kinematic data, measuring knee flexion/extension, abduction/adduction, and internal/external rotation, are increasingly used in gait analysis towards quantifying the knee function [1], understanding pathological knee alterations [2], and assessing the progression of knee pathologies and their impact on the gait [3, 5]. They also offer opportunities for diagnostics [6], classification [7], and therapy of knee musculoskeletal pathologies [8]. Kinematic data are generally given in the form of normalized curves of measurements recorded on a treadmill at regular intervals of time during a gait cycle. Several studies have used knee kinematic data to obtain crucial information about musculoskeletal pathologies [9], to distinguish between knee osteoarthritis and asymptomatic subjects [10], and to further

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classify osteoarthritis populations with respect to the pathology level of severity [4, 7, 11, 12]. These studies have generally reported, without mentioning specifically the gender corresponding to data measurements, that the high dimensionality of kinematic data, their significant intra-class variability and interclass proximity, usually make their analysis a difficult task. However, no study has attempted to explain this difficulty in terms of objective metrics of data complexity. Instead, informal assessments have been generally invoked to deem knee kinematic data as “simple” or “complex,” using classification rates obtained with a common classifier believed to be appropriate for the type of application at hand [7, 11]. Although such a characterization can be sometimes useful, it does not afford a general, objective, and practical means of assessing the complexity of the data. In this study, we use classifier independent data complexity metrics to evaluate how difficult it can be to classify knee kinematic data.

The design and study of data complexity metrics is an emergent subject in data mining and classification. In this context, complexity measures that correlate linearly with classification error have been investigated in [13, 14]. By examining the performance of several classifiers in a space defined by complexity measures, the studies in [15, 16] were able to build a model of a classifier accuracy based on the data complexity measures divided into three general types: (1) class ambiguity, to characterize the overlap of classes in feature space. This is in general due to class representation features that cause ambiguous interpretations. The study [17] gives a lower bound on the achievable error rate in this case; (2) boundary complexity, related to the Kolmogorov complexity [18, 19], defined as the minimum length of a computer program needed to reproduce the class boundary: a classification problem is complex if it takes a “long” algorithm to describe the class boundary. Because the Kolmogorov complexity is algorithmically uncomputable [20], approximate measures are used which describe geometrical properties of data sets. Such measures, which depend on the data set only, can guide the selection of appropriate classifiers; and (3) geometry and density of manifolds, which describe sample sparsity, and feature space dimensionality.

This study investigates such complexity metrics to evaluate knee kinematic data complexity, and does so for both *single features*, i.e., features considered individually, and *global features*, i.e., for multiple features taken simultaneously. The data describe the temporal variation of the three dimensions of knee rotation during locomotion, namely knee flexion/extension, abduction/adduction, and internal/external, in pathology classification problems involving knee osteoarthritis. Osteoarthritis (OA) is the most common type of musculoskeletal disorder and the knee is one of the most affected joints [21]. The kinematic data have interesting characteristics: (i) they reflect the functional status of the knees, (ii) they are objective non-invasive measurements and non-radiant like conventional static X-ray imaging and, (iii) they can be used further by health care professionals to personalize, and therefore enhance, care pathways of knee OA patients. Traditionally, kinetic (rather than kinematic) variables, the external knee adduction moment in particular, have been used in the assessment of the progression and severity of knee OA. However, their measurement needs sophisticated setups, which are, generally, available only in specialized gait study laboratories (Simon 2004). Kinematic data, instead, are acquired in a normal clinical setting, using a commercially available treadmill and a simple non invasive knee attachment system.

Materials and methods

Knee kinematic data collection

Analysis of 3D knee kinematic data measurements, consisting of the temporal variation of the three dimensions of knee rotation, namely the rotation angles measured in the sagittal, frontal,

and transverse planes during a full gait cycle (Fig 1), serve knee pathology classification algorithms [22] and can subsequently guide OA therapy plans [8].

The data used in this study was collected, for research projects [3, 23, 24], using a state-of-the-art KneeKG acquisition system. The accuracy and reproducibility of the system have been assessed in several studies [25–27]. For each subject, the positional angles are recorded during two walking trials of 25 sec on a treadmill. For each participant patient, current methods of analysis have used the average of about a dozen curves in the set of measurement curves, so chosen as to maximize a correlation criterion between classes, namely the Inter Class Correlation Index of the observations [28]. In our study, a series of fifteen (15) full gait cycle walks on the treadmill are averaged to obtain a representative mean pattern per subject based on an adjusted coefficient of multiple determinations [29]. This is followed by interpolation and re-sampling from 1% to 100% of the gait cycle, therefore giving 100 measurement points for each participant. This yields a significant amount of high-dimensional data, leading to “the curse of dimensionality,” in classification [30]. Also, knee pathologies notoriously cause high within-class variability and in-between class similarity (example in Fig 1).

The data collection was approved by institutional ethics committees of the University of Montreal Hospital Research Center (Reference numbers CE 10.001-BSP and BD 07.001-BSP) and of the École de technologie supérieure (Reference numbers H20100301 and H20170901). All subjects provided written informed consent before the studies began. We used 3D knee kinematic data from two groups. The first group included 40 patients with knee OA diagnosed according to clinical and radiographic criteria defined by Altman et al. [31]. The patients were excluded if they had vestibular, neurological, or musculoskeletal disorders, fracture of the lower extremity, rheumatoid arthritis, or generalized osteoarthritis, limping gait or any condition that could affect a treadmill walking evaluation. The second group, which formed the control group, contains 40 asymptomatic participants (AS). Table 1 summarizes the participants’ demographic characteristics and their walking speed. A statistical *t*-test was performed to compare the two groups characteristics using SPSS 18.0 (Statistical Package for Social Sciences) (SPSS Inc. Released, 2009. PASW Statistics for Windows). A threshold of significance set at $p = 0.05$ shows that there is no statistical difference between the two groups except for the height variable.

Features Extraction on 3D Knee kinematic data

A set of 62 biomechanical features are extracted from these 3D kinematic patterns for data complexity analysis. The features chosen are biomechanical parameters routinely assessed in clinical biomechanical studies of knee OA populations; for instance, maximum, minimum, varus and valgus thrust, angles at initial contact, mean values and range of motion (ROM) throughout gait cycles or specific gait sub-cycles (i.e., loading, stance, swing, etc.) [2, 3, 32]. The 3D knee kinematic data were normalized to remove dependence on magnitude and scale.

Knee kinematic data complexity

Data complexity is evaluated on the descriptive biomechanical features according to both single features and global features complexity metrics. The first metric evaluates the overlap of individual feature measurements whereas the latter evaluates the separability of classes and the geometry of the manifolds spanned by each class when the features are considered simultaneously.

Single feature complexity. Complexity of a single feature informs us on that particular feature discriminant power, i.e., its capacity to distinguish data samples from distinct classes. Such a characterization is useful for clinical assessments. Indeed, it allows the study of specific

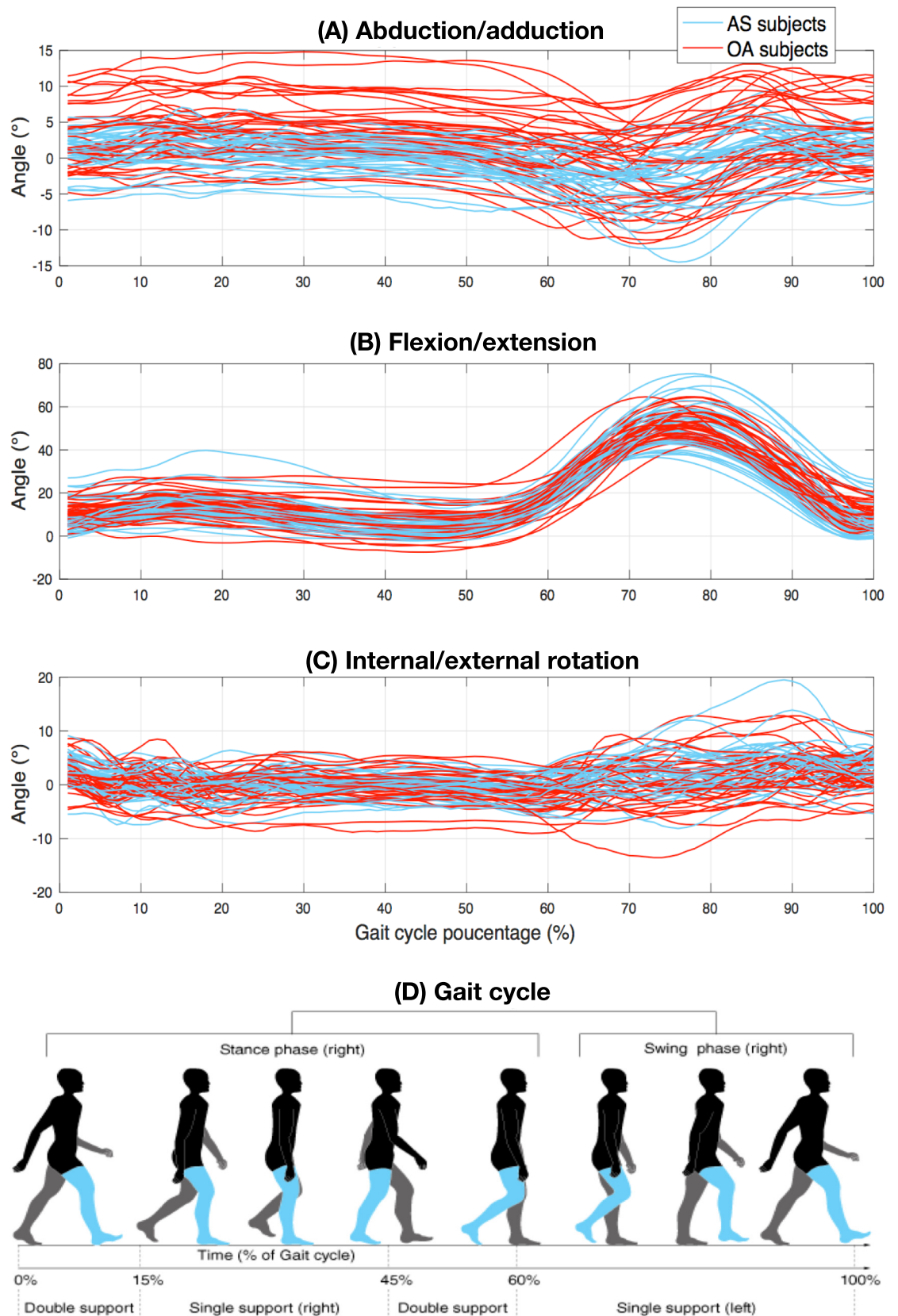


Fig 1. Measures of class overlap in feature space: (A) Abduction/adduction (B) Flexion/extension, and (C) Internal/external rotation. The signals were interpolated and resampled from 1% to 100% (100 points) of the gait cycle. Each red curve represents an OA subject and each blue curve represents an AS subject (D) The gait cycle phases.

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Table 1. General subject characteristics.

	OA group	AS group
	N = 40	N = 40
Age (year)	62.4 ± 8.2	48.6 ± 17.47
Height(m)	1.61* ± 0.09	1.67 ± 0.10
Weight (kg)	82.28 ± 18.84	69.70 ± 11.87
BMI (kg / m2)	31.20 ± 5.59	24.69 ± 3.05
Walking speed (m/s)	1.31 ± 0.96	2.47 ± 1.42
Proportion of women	72%(24)	16%(10)

* Significant difference between groups with a $p < 0.05$

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kinematic points of interest, having a clinical meaning, in order to correlate them with typical knee function behavior.

For each individual feature, the following three metrics examine the range and spread of the values of instances from distinct classes. Specifically, let $\mathcal{D} = \{\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_n\}$ be a data set containing n knee kinematic data measurements, each belonging to one of two distinct classes c_1 and c_2 . Each element \mathbf{x}_i is characterized by a feature vector (f_1, f_2, \dots, f_p) , where p is the dimension of the feature space. In our case $p = 62$. The complexity metrics are:

- Fisher discriminant ratio (F1): for a two-class data set, ratios $F1 = \{F1_1, F1_2, \dots, F1_p\}$ for feature f_i , ($i = 1, \dots, p$), are defined as:

$$F1_i = \frac{(\mu_{i1} - \mu_{i2})^2}{(\sigma_{i1}^2 + \sigma_{i2}^2)}, \tag{1}$$

where $\mu_{i1}, \mu_{i2}, \sigma_{i1}, \sigma_{i2}$ are the means and variances of the two classes, respectively, according to the i^{th} feature, ($i = 1, 2, \dots, p$). The range of $F1_i$ is $[0, +\infty[$. Small values indicate strong class overlap. High values indicate good class separation when using the i^{th} feature.

- Volume of overlap region (F2): This measure estimates the amount of relative overlap of the bounding regions of two classes [33]. Let $\max_{i1} = \max(f_i, c_1)$, $\max_{i2} = \max(f_i, c_2)$, $\min_{i1} = \min(f_i, c_1)$, $\min_{i2} = \min(f_i, c_2)$ the maximum and minimum values of each feature f_i in the classes c_1 and c_2 . For two-class data sets, the ratio $F2_i$ for each feature f_i , ($i = 1, 2, \dots, p$) is computed as:

$$F2_i = \frac{\min(\max_{i1}, \max_{i2}) - \max(\min_{i1}, \min_{i2})}{\max(\max_{i1}, \max_{i2}) - \min(\min_{i1}, \min_{i2})} \tag{2}$$

The range of $F2$ is $[0, 1]$. Larger values indicate larger class overlap, and higher data complexity thereof. A shortcoming of this measure is that a single feature with non-overlapping regions causes $F2$ to be zero.

- Feature efficiency (F3): this measure is particularly relevant when dealing with high-dimensional data. It informs on how much each feature contributes to the separation of the classes, and the contribution is called efficiency. For each feature, the ambiguous (overlapping) regions are removed so that only non-overlapping regions remain for consideration. Let $\text{MinMax}_i = \min(\max(f_i, c_1), \max(f_i, c_2))$ and $\text{MaxMin}_i = \max(\min(f_i, c_1), \min(f_i, c_2))$. For

each feature f_i , let Q_i be the following ratio:

$$F3_i = \frac{|f_i \in [\text{MinMax}_i, \text{MaxMin}_i]|}{n}, \tag{3}$$

where $| |$ denotes the number of non-overlapping elements and n is the total number of elements in both classes. When there is no overlap between classes, $F3_i$ achieves the maximum value of 1.

Each single feature complexity metric requires the estimation of high and low thresholds to assess whether the feature is complex or not. We estimated the various thresholds based on the probability distributions of the feature complexity measures. For each metric, i.e., the Fisher discriminant ratio $F1_i$, the volume of overlap region $F2_i$, and the feature efficiency $F3_i$, the best-fitting distribution is determined by the maximum likelihood estimation. The thresholds are subsequently estimated using the rule of thumb of 5th and 95th quantiles of the probability distribution.

Global feature complexity. The global feature complexity is based on the following metrics: fraction of points on the class boundary (N1), ratio of average intra/inter class nearest neighbor distance (N2), error rate of a nearest neighbor distance (N3), fraction of maximum covering spheres (T1), average number of points per dimension (T2).

- Fraction of points on the class boundary (N1): This measure estimates the length of the class boundary. The minimum spanning tree (MST) connecting all the training samples is generated and the fraction of points of a class connected to the opposite class is computed [34, 35]. The range of N1 is [0, 1]. Large values indicate that the majority of points lay closely to the class boundary, which can make it difficult to locate the class boundary accurately.
- The ratio of average intra/inter class nearest neighbor distance (N2): Let \mathbf{x}_i denote an input sample, $i = 1, 2, \dots, n$, where n is the number of samples. Let $\text{IntraDist}(\mathbf{x}_i)$ designate the distance between \mathbf{x}_i and its nearest neighbor within the class, and $\text{InterDist}(\mathbf{x}_i)$ the distance to its nearest neighbor of the other class. The ratio of average intra/inter class nearest neighbor distance (N2) is the ratio of the sum of the intra-class distances to the sum of the inter-class distances for each input example:

$$N2 = \frac{\sum_{i=0}^n \text{IntraDist}(\mathbf{x}_i)}{\sum_{i=0}^n \text{InterDist}(\mathbf{x}_i)} \tag{4}$$

- Leave-one-out error rate of the Nearest neighbor classifier (N3): This measure informs on how close the samples of different classes are. It returns the leave-one-out error rate of the Nearest neighbor classifier.
- Nonlinearity of the Nearest neighbor classifier (N4): This measure creates a test set and computes the test error of the Nearest neighbor classifier. The range of N4 is [0, 1]. Low values indicate low error by linear separation.
- Fraction of maximum covering spheres (T1): This measure describes the shapes of class manifolds using the notion of adherence subset [36]. An adherence subset is a sphere centered on an sample of the data set which is grown as much as possible before touching any sample of another class. The T1 is measured based on the number of spheres normalized by the total number of points.
- Average number of points per dimension (T2): The average number of points per dimension is the ratio of the number of elements in the data set to the number of features. Its value is a rough indicator of sparseness of the data set.

Statistical analysis. Following individual feature complexity evaluation, we performed a *t*-test statistical analysis to assess feature dissimilarity between the two groups (osteoarthritis patients and control participants). Since each feature single complexity variable informs on that particular feature discriminant power, i.e., its capacity to distinguish data samples from distinct classes, our hypothesis is that the features retained by complexity analysis as discriminant are statistically different in the two groups. A *P*-value of 0.05 was set as the statistical level of significance.

Results and discussion

We recall that data complexity assessment used 40 osteoarthritis patients (OA) and 40 control participants (AS). A set of 62 biomechanical features ($p = 62$) routinely assessed in clinical biomechanical studies of knee OA populations have been selected (as described in section Features Extraction on 3D Knee Kinematic Data). The analysis was done using Matlab R2017a software (Mathworks, Massachusetts, United State).

Single feature complexity

The single feature complexity measures have been evaluated using Fisher discriminant ratio (F1), the volume of overlap region (F2), and the individual feature efficiency (F3). The threshold values have been identified, for each complexity metric, using a probability density which best fit the complexity data.

[Fig 2](#) indicates that the Fisher discriminant ratio F1 and the feature efficiency F2 best follow a Weibull distribution, and the volume of overlap region F3 follows a normal distribution. [Table 2](#) summarizes the thresholds value determined using the 10th and 90th percentiles of each complexity measure empirical density.

The single complexity measures of each feature and the corresponding thresholds are presented in [Fig 3](#). [Fig 3A](#) represents the discriminant ratio $F1_i$ for each feature f_i ($i = 1, 2, \dots, 62$) computed according to [Eq 1](#). Its threshold was set to 0.33 because we are interested in high values of $F1_i$ ([Table 2](#), line 1). Except for the set of features $\{f_1, f_2, f_3, f_6, f_7, f_{11}, f_{57}\}$, the low values of $F1_i$ demonstrate the low discriminative power of the 3D kinematic features.

In [Fig 3B](#), we represented the ratio of the width of the overlap interval $F2_i$ of each feature. The threshold here was set to 0.47 because, for this metric, we are interested in low value of $F2_i$ ([Table 2](#), line 2). The ratio values are generally high except for features $\{f_1, f_3, f_{57}, f_{58}\}$. Finally, in [Fig 3C](#), we represented the feature efficiency. The low values of $F3_i$ show that the ratio of the number of samples that are not in the overlapping region to the total number of samples is low except for features $\{f_3, f_7, f_{26}, f_{27}, f_{28}, f_{32}, f_{49}, f_{57}\}$.

Although the identified features for each complexity metric are different, there is overlap between some of them. For instance, feature f_3 is discriminant according the three complexity metrics. Same for the feature f_1 et f_{65} which is discriminant according both the Fisher discriminant Ratio (F1) and the individual feature efficiency (F3). As a result of the single complexity analysis, the discriminant features are given by the following set of 13 features: $\{f_1, f_2, f_3, f_6, f_7, f_{11}, f_{26}, f_{27}, f_{28}, f_{32}, f_{49}, f_{57}, f_{58}\}$.

Statistical analysis

Following the single feature complexity analysis, we performed a statistical *t*-test analysis to examine the differences between the two groups (the osteoarthritis patients (OA) and the control participants (AS)) of these 13 retained features. [Table 3](#) summarizes their clinical meaning and their corresponding *p*-value. The results of the statistical analysis confirms those obtained using the complexity analysis. Indeed, the retained 13 features are statistically significantly

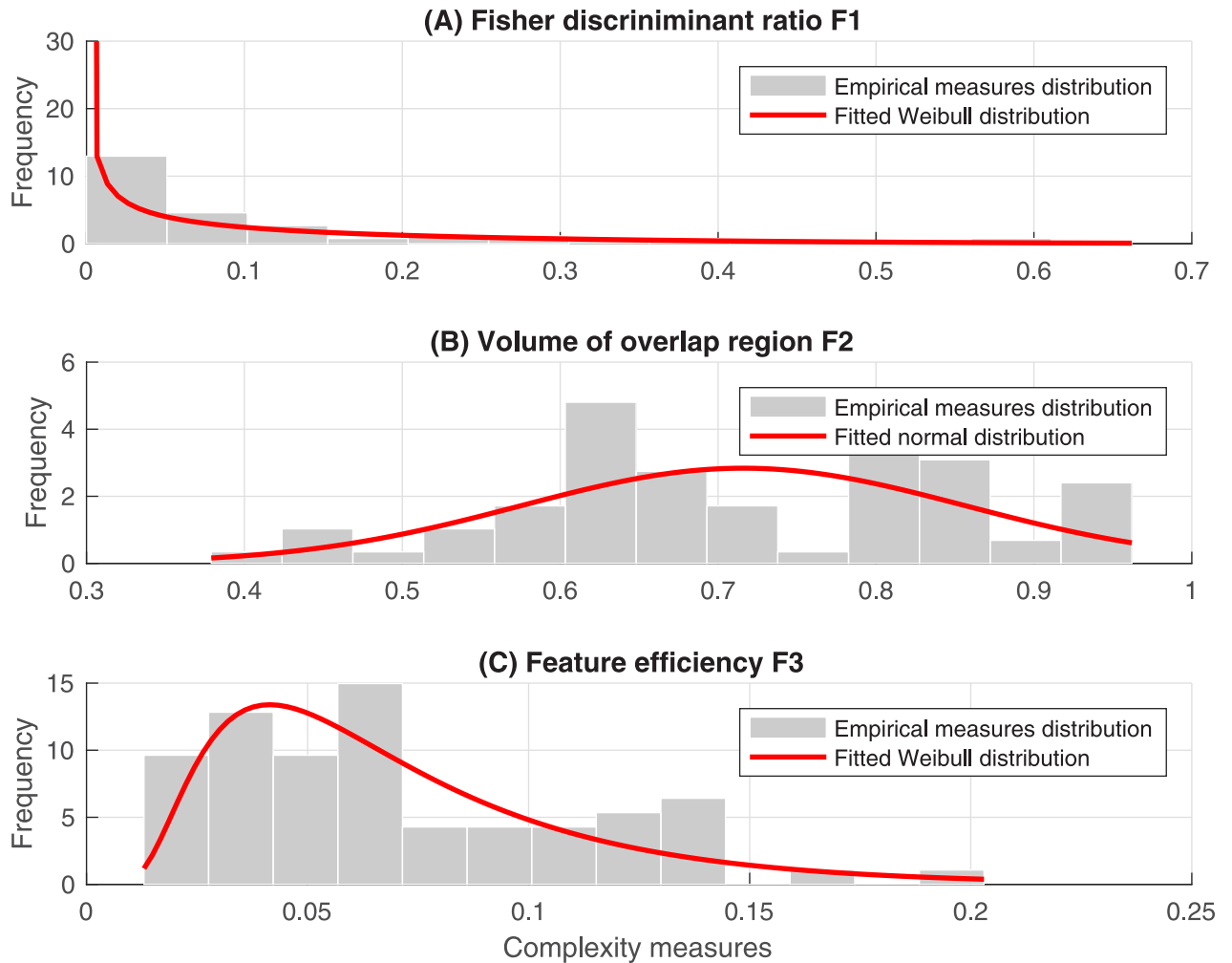


Fig 2. Empirical distribution of the class ambiguity measures (A) The Fisher discriminant Ratio F1, (B) The ratio of the width of the overlap interval F2 and (C) The individual feature efficiency F3. The red curves are the corresponding fitted distribution function.

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different, and can therefore be considered discriminant of OA patients and AS participants ($p < 0.001$).

Both statistical analysis and single complexity analysis support previous studies on bio-mechanical data and their association with knee pathologies. Indeed, the features f_1, f_2, f_3 and f_{11} which are related to the varus or valgus thrust during loading phase, have been identified as the most useful parameter, serving as a diagnostic biomarker [3, 21]. Also the feature f_{57} , which corresponds to the range of motion during loading phase, has been identified as a part of burden of disease biomarkers to discriminate between moderate OA grades and severe OA

Table 2. Thresholds for single feature complexity.

Complexity metrics	Low and High thresholds
Fisher's Discriminant Ratio (F1)	{0.00, 0.33}
Volume of overlap region (F2)	{0.47, 0.99}
Feature efficiency (F3)	{-0.02, 0.13}

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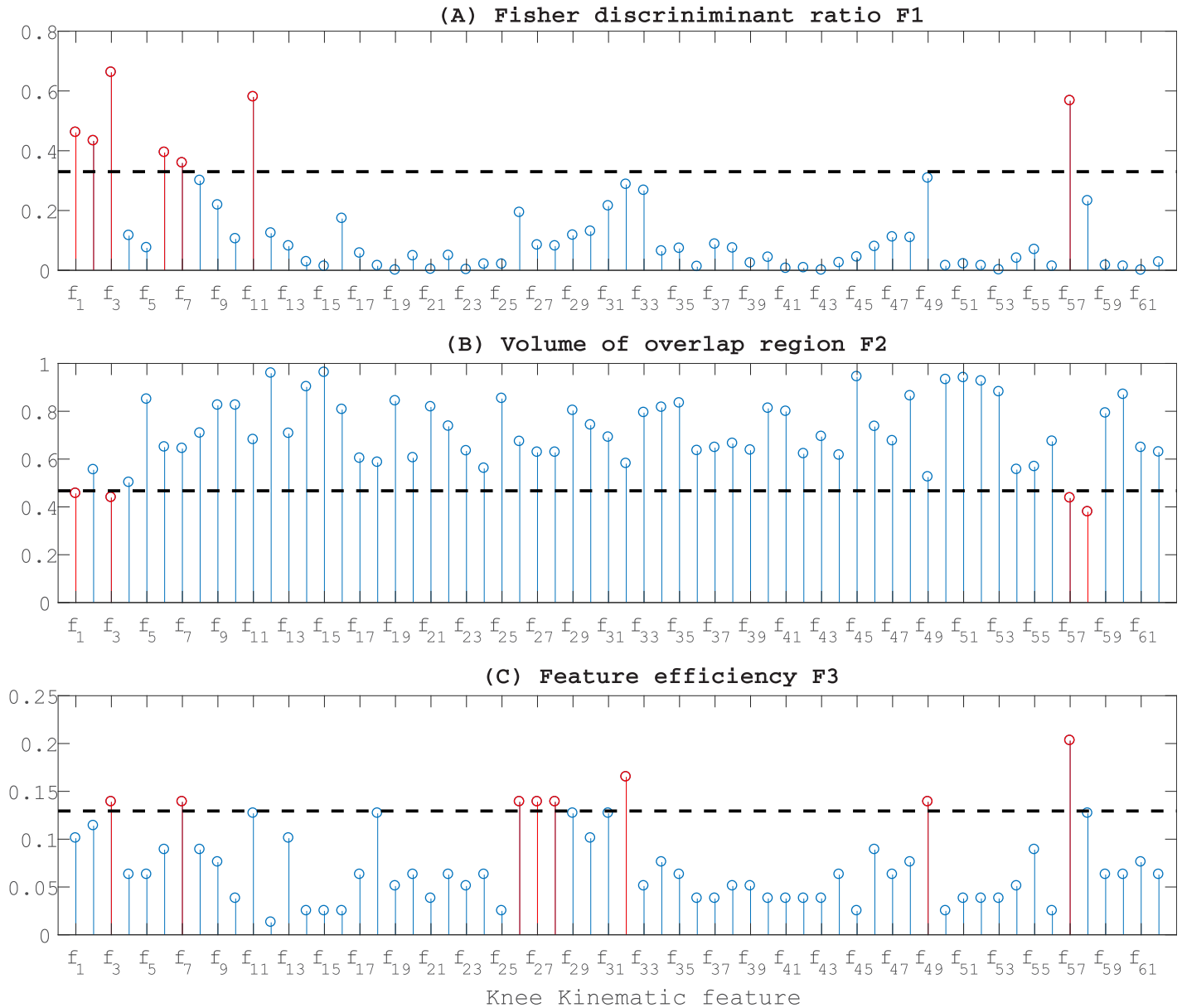


Fig 3. Measures of single feature complexity for feature f_i ($i = 1, 2, \dots, 62$): (A) The Fisher discriminant Ratio F1; a high value of F1, indicates that the feature is discriminant. (B) The ratio of the width of the overlap interval F1; a low value of F2, measure means that the feature can discriminate the samples of different classes. (C) The feature efficiency F3; a high value of F3, indicates a good efficiency. The horizontal dotted black lines correspond to the threshold values of each single feature complexity. The red vertical lines correspond to the retained discriminant features while the blue ones correspond to the features having high complexity.

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grades [3]. Another study compared a set of biomechanical parameters in patients categorized as moderate to severe OA grades [21, 37]. It was reported that both peak knee adduction moment and knee adduction angular impulse increased with knee radiographic grade.

Global feature complexity

The global feature complexity metrics have been measured using: the Fraction of points on the class boundary (N1), the Ratio of average intra/inter class nearest neighbor distance (N2), the

Table 3. Features arising following single feature complexity analysis.

Selected features	p-value
f_1 : Varus thrust during loading (1% to 20% of GC)	0.000
f_2 : Varus thrust during loading (1% to 10% of GC)	0.000
f_3 : Varus thrust during loading (1% to 30% of GC)	0.000
f_6 : Mean abduction angle during stance phase	0.000
f_7 : Mean abduction angle during mid stance and terminal stance phase	0.001
f_{11} : Valgus thrust during loading (1% to 30% of GC)	0.000
f_{26} : Maximum of the adduction/abduction angle	0.01
f_{27} : Minimum of the adduction/abduction angle	0.04
f_{28} : Minimum of the adduction/abduction angle during swing phase	0.04
f_{32} : Adduction/abduction angle at 20% of GC	0.003
f_{49} : Adduction/abduction angle absolute value at 20% of GC	0.000
f_{57} : Range of motion during loading	0.000
f_{58} : Range of motion absolute value during loading	0.001

Significant difference between groups with a $p < 0.05$

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Error rate of a nearest neighbor distance (N3), the Fraction of maximum covering spheres (T1), the Average number of points per dimension (T2).

Table 4 summarizes these metrics. It shows high values of the ratio of average intra/inter class nearest neighbor distance ($N2 = 0.95$); this indicates that samples from the same class are dispersed. This result is confirmed by the fraction of points on the class boundary ($N1 = 0.54$) which shows that an important number of samples are located near the class boundaries. As a result the nearest neighbor error rate ($N3 = 0.42$) approaches that of random classification. Moreover, the analysis of the global complexity metrics shows the sparsity of the features. Indeed, the fraction of maximum covering spheres is equal to 1 ($T1 = 1$), which means that the largest adherence subset is one sample. Moreover, the average number of points per dimension ($T2 = 1.29$) indicates high sparseness of the data set. This sparsity is an important problematic in classification [30].

Table 1, which describes the general subject characteristics, shows that the proportion of women with respect to that of men is higher in the OA group (72% of women against 38% of men) while it is lower in the AS group (16% of women against 84% of men). For further analysis, to take into account gender, we measured the data global complexity for men and women separately to determine if it is gender-dependent. Table 5 summarizes the complexity results per gender. Overall, global complexity is high in both disease groups when analyzed separately per gender, thus confirming the conclusions drawn from Table 4. Moreover, the complexity is

Table 4. Global complexity metrics of 3D knee kinematics.

Complexity measures	Values
Fraction of points on the class boundary (N1)	0.5
Ratio of average intra/inter class nearest neighbor distance (N2)	0.95
Error rate of a nearest neighbor distance (N3)	0.36
Non-linearity of 1-nearest neighbor classifier (N4)	0.20
Fraction of maximum covering spheres (T1)	1
Average number of points per dimension (T2)	1.29

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Table 5. Global complexity metrics of 3D knee kinematics according the gender.

Complexity measures	Men group	Women group
Fraction of points on the class boundary (N1)	0.42	0.55
Ratio of average intra/inter class nearest neighbor distance (N2)	0.87	0.93
Error rate of a nearest neighbor distance (N3)	0.24	0.42
Non-linearity of 1-nearest neighbor classifier (N4)	0.06	0.20
Fraction of maximum covering spheres (T1)	1	1
Average number of points per dimension (T2)	0.47	0.68

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Table 6. Complexity metrics of 3D knee kinematics and reference databases.

Complexity measures	3D knee kinematics	Wine	Iris
Fraction of points on the class boundary (N1)	0.5	$4.7 \cdot 10^{-4}$	0.6
Ratio of average intra/inter class nearest neighbor distance (N2)	0.9	0.026	0.1
Error rate of a nearest neighbor distance (N3)	0.3	$2.3 \cdot 10^{-4}$	0
Non-linearity of 1-nearest neighbor classifier (N4)	0.2	0.0	0
Fraction of maximum covering spheres (T1)	1	1	1
Average number of points per dimension (T2)	1.29	522	37.5

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higher for women than men. This explains recent literature [38, 39] reporting more effective automatic classification in men’s groups than in women’s.

Comparison to the complexity of other types of data

We compared the knee kinematic data complexity measures to those obtained using the data in two public databases for classification tests: the *Wind database*, which contains 178 samples from two classes described by 13 features, and the *IRIS database*, which contains 150 samples from two classes described by 4 features (Table 6).

The ratio of average intra/inter class Nearest neighbor distance (N2) shows that the discriminant power is higher for Wine and IRIS than for the knee kinematic data. Indeed, N2 is 0.9 for the kinematic data, 0.026 for Wine, and 0.1 for IRIS. Also, the average number of points per dimension (T2) is very low for knee kinematic data. This indicates that 3D knee kinematic data is significantly more complex compared to that of IRIS and Wind data.

Conclusion

This study investigated 3D knee kinematic data complexity using both single feature and global feature complexity metrics. The first evaluates the overlap of individual feature measurements, whereas the latter measures the separability of classes and the geometry of the manifolds spanned by each class when the features are considered simultaneously. The results reveal that knee kinematic data are sparse and highly complex and, thus, foretell the difficulty of knee pathology classification. Indeed, from the initial set of 62 biomechanical features, only 13 features have been identified as not complex. Such information might be useful in future work (1) in the selection of an appropriate classification algorithm and for the interpretation of classification rates and, (2) in clinical studies to identify biomarkers for knee pathologies.

Author Contributions

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Visualization: Youssef Ouakrim.

Writing – original draft: Neila Mezghani.

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